AComprehensiveReviewofShortestPathAlgorithmsfor Network Routing

Abstract

Therapiddevelopmentofdigitaltechnologyandtheincreasinginterconnectionofdeviceshavemade computer networks indispensable to modern life. Global data movement, communication, and applications like cloud computing, IoT, e-commerce, and smart cities are all made possible by these networks.Routingalgorithms particularlyshortest path algorithms arecrucial fordeterminingthemost effective data transmission routes and are largely responsible for the dependability and efficiency of these networks. Because these algorithms maintain stability and reliability while lowering latency, costs, and energy consumption, they are crucial to network operation.

Shortestpathproblemsolvinghaslongreliedonfundamentalalgorithmswithoriginsingraphtheory, such as Bellman-Ford and Dijkstra's. Despite their successes, the growing complexity and dynamic nature of contemporarynetworks have exposed their shortcomings. Advanced approaches, including heuristic, hybrid, and AI-driven methods, have been developed to get around these challenges. Innovationslikeantcolonyoptimizationandblockchain-basedalgorithmshaveimprovedcomputing efficiency, security, and adaptability.

The Internet of Things, VANETs, and SDNs are just a few of the domains that use these algorithms; each has specific requirements, like real-time adaptation and energy efficiency. Reinforcement learningandpredictionmodelsdrivenbymachinelearninghave furtherincreasedroutingefficiency, while simulation tools such as Mininet and OMNeT++ have been essential for evaluating algorithm performanceinpracticalscenarios. Asemergingtechnologieslikeblockchainandquantumcomputing become more widely accepted, shortest path algorithms will continue to advance, ensuring their suitabilityin the rapidly evolving digital environment. This study, which looks at their development, applications, and possible future directions, emphasizes their importance increating modernnetworks.

Keywords: ShortestPathAlgorithms, NetworkOptimization, Dijkstra'sAlgorithm, Bellman-Ford Algorithm, Heuristic Algorithms, A*, Ant Colony Optimization (ACO), Hybrid Algorithms.

1. Introduction

As digital technology has grown exponentially and gadgets have become increasingly networked, computer networks have become indispensable to modern life. These networks are essential for international communication and data transfer in a variety of applications, including cloud computing, commerce, the Internet of Things, and smart cities. The efficiency and reliability of these networks depend heavily on routing algorithms, and shortest path techniques are necessary to reach optimal performance. These algorithms determine optimal data transmission channels by reducing critical characteristics such as latency, cost, and energy consumption while maintaining network reliability and stability [1], [2]. Shortest path algorithms are based on the foundation of graph theory, which depicts networks as graphs composed of nodes (representing devices) and edges (representing connections).BasicalgorithmssuchasBellman-Ford[4]andDijkstra's[3]werethefirsttotacklethe singlesource shortest path problem. Due to their efficiency and ease of use, these conventional techniques are still widely used to day and have formed the basis of modern routing protocols. Bellman-interval and the state of theFord, for instance, has provent oberobustin situations when edge weights are negative, and Dijkstra's technique is crucial for link-state routing protocols [4],]. With the increasing sophistication and breadth of networks, traditional shortest path approaches have faced challenges in handling resource constraints, large datasets, and shifting topologies. To address these problems, researchers have developed complex algorithms that incorporate heuristics, hybrid approaches, and artificial intelligence (AI). While ant colony optimization [6] takes advantage of natural foraging behavior to determine the optimal routes, block chain-based solutions enhance routing security by providing transparentandunchangeablepathdecisions[7].Withtheseadvancements, algorithms may now adapt dynamically to changing network conditions and increase computational efficiency.

Many diverse fields, each with its own set of requirements and restrictions, use the shortest path algorithm. In InternetofThingssystems, energy-efficientalgorithms arecrucialforextendingdevice lifetimesandensuringsustainablenetworkoperation, as devices often have limited resources [8]. Ina similar vein, real-time decision-making algorithms are required for vehicle ad hoc networks (VANETs) to manage high mobility and traffic. Software-defined networks (SDNs) benefit from adaptive routing algorithms because they can adjust routes dynamically in response to network congestion and traffic patterns [5]. Advances in AI have further changed the methods used for the shortest paths. Thanks to reinforcement learning (RL) models, routing algorithms can now adapt dynamically to changes in the network in real time, improving efficiency and reducing latency [10]. Additionally, machine learning (ML)-powered prediction models have simplified anticipatory congestion management by optimizing routing decisions even in highly dynamic scenarios [11]. Researchers have tested and assessed these algorithms in simulation environments such as Mininet and OMNeT++ [12], which allow them to see how well they perform in practical settings.

There are still few problems despite these advancements. Modern network algorithms must be able to process vast volumes of real-time data, hand let remendous sizes, and adapt to shifting security threats.

With billions of devices connecting simultaneously in scenarios like smart cities and industrial IoT, ensuring efficient and safe routing is a difficult undertaking. Strong security measures must also be included in routing algorithms to combat risks like data interception and route hijacking [7]. As the digitalworldevolves, these archforthe best pathalgorithms is at the fore front of networking research.

Futuretechnologiessuchasquantum computingcouldrevolutionizepathoptimizationbyfacilitating faster and more scalable solutions. New decentralized and secure routing paradigms are being presented by blockchain technology. By overcoming current limitations and leveraging these developments, shortest path algorithms are poised to remain at the forefront of the development of both modern and future networks. This study investigates the concepts, historical development, and recent advancements in shortest path algorithms for network routing. Through the resolution of significant problems, the presentation of innovative solutions, and the discussion of practical applications, this book highlights the significance of these algorithms in assessing the dependability and effectiveness of contemporary computer networks.

2. Backgroundtheory

2.1 ShortestPathAlgorithmClassification

Thethreeprimarycategoriesofshortestpathalgorithmsarehybrid,heuristic,andclassical.traditional algorithms,suchasFloyd-Warshall,Johnson's,andDijkstra'sBellman-Ford.Heuristicalgorithmslike GreedyBest-FirstSearch,AntColonyOptimization,andA*.Theadvantagesofheuristicandclassical approaches are combined in hybrid algorithms.

2.1.1 classicalAlgorithmsfortheShortest Path.

Deterministictechniquesknownasclassicalalgorithmsensurethebestanswerstoshortestpathissues. Examples include Bellman-Ford, which can handle distributed computations with negative weights, and Dijkstra's, which is appropriate for graphs with non-negative weights. They serve as the cornerstone of reliable and effective network routing.

A-TheDijkstra Algorithm

Findingtheshortest paths in networkgraphs is acommon useofDijkstra's Algorithm, abasictool in computer networking. Its ability to determine the optimal data transmission routes while lowering characteristics like cost, latency, or resource consumption accounts for its significance in network routing. Edsger W. Dijkstra developed the method in 1959 with the goal of figuring out the shortest path between a single source node and each other node in a network with non-negative edge weights [3].Itiscurrentlyabasicpartofmanyroutingprotocolsduetoitsfeatures,whichenablereliableand efficient communication in a range of network scenarios [1]. In the context of network routing, networksaredepictedasgraphs,wherenodesrepresenthardwaresuchasswitchesorroutersandedges representlinksorconnectionsbetweenthem.Eachedgehasaweight,whichcouldrepresentlatency, bandwidth use, orphysical distance. Dijkstra's Algorithm finds the shortest path treefrom the source node to all other nodes, allowing network devices to forward data packets along the most efficient paths [2].

ShortestPathAlgorithms

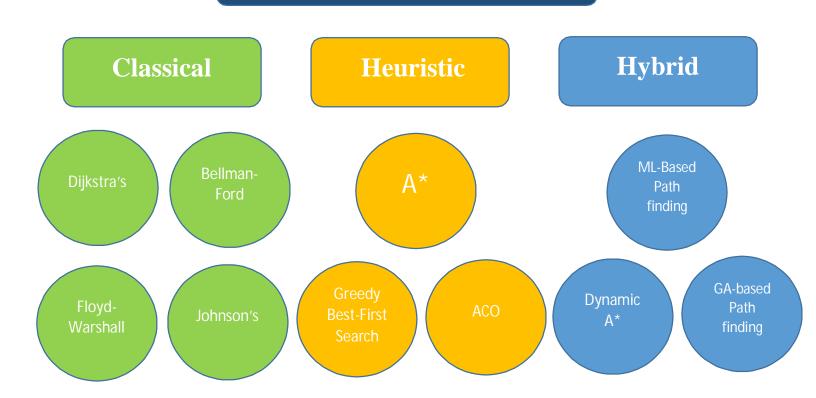


Figure1-Shortestpath Algorithmsclassification

The method involves keeping a set of nodes with known shortest paths and another set of nodes that havenotbeenvisited.Initially, it assigns a distance of zero to the source node and an infinite distance to each subsequent node. Using a priority queue, its elects the unvisited node with the shortest distance, marking it as visited and updating the distances of its neighbors if a shorter path is found. This method is done recursively until all nodes are visited or the fast est path to a specific target node is found. Thegreedy technique expands the shortest paths at each step, ensuring optimal solutions for graphs with nonnegative edge weights [2], [3]. Dijkstra's Algorithm is heavily utilized in network routing protocols, particularly link-state protocols such as OpenShortestPathFirst(OSPF). InOSPF, routers use Dijkstra's Algorithm to find the shortest path tree using link-state ads that show the current conditionofthenetwork.Byprovidingrouterswiththeoptimalpathsforforwardingdatapackets,this tree guarantees efficient and loop-free routing. Outside of OSPF, the technique serves as the foundation for trafficengineering applications and other network optimization initiatives, where it aids indynamictrafficmanagementtominimizecongestionandoptimizeresourceuse[5]. Theability of

Dijkstra's Algorithm to generate reliable and deterministic results, ensuring consistent routing decisions, isoneofitsbenefits innetworkrouting. Its efficiency allows it to scale to medium-to-large networks, particularly when combined with complex data structures like Fibonacci heaps [13]. However, the method has certain limitations, especially in dynamic networks with dynamic topologies. Pathways must be fully recalculated by the program after changes in these settings, which can be computationally expensive. Furthermore, its limitation to graphs with non-negative edge weights limits its applicability incertain networks cenarios where costs may fluctuate in an unpredictable way [9]. Despite these challenges, Dijkstra's Algorithm remains an essential tool for network routing because it forms the foundation of increasingly complex and adaptable routing systems. As demonstrated by its continued applicability in modern networking, it is a crucial algorithm for understanding and enhancing network communication [11][16].

B-Bellman-Ford algorithm

TheBellman-Fordalgorithmisagraphsearchtechniquethatfindstheshortestpathbetweenaspecific source vertex and each other vertex in the graph. This method can be applied to both weighted and unweighted graphs. Similar to Dijkstra's shortest path algorithm, the Bellman-Ford method is guaranteedtofindtheshortestpathinagraph.Bellman-FordismoreadaptablethanDijkstra'smethod sinceitcanhandlegraphswithnegativeedgeweights, evenifitiss lower. It is crucial to keep inmind that in a graph with a negative cycle, there isn't a shortest path. If the road continued to circle the negative cycle indefinitely, the cost would decrease even if the journeyduration increased. Bellman- Ford thus has the added advantage of being able to recognize negative cycles. Unlike Dijkstra's algorithm, which uses a greedy approach, Bellman-Ford uses a dynamic programming paradigm, iterating through all edges up to |V| - 1 times, where |V| is the number of vertices in the graph. By periodically relaxing each edge, the method continuously improves the shortest pathway estimations. This makes it particularly suitable for applications where negative weights might be present, such network routing and financial market arbitrage detection. However, because to its higher temporal complexity of O(VE), where V is the number of vertices and E is the number of edges, Bellman-Ford is usually only used when negative weights are present. Additionally, the algorithm's ability to detect negative weight cycles ensures its reliability in scenarios when they could lead to unstable calculations [4].

B.1HowBellmanFord'salgorithmworks

Overestimating the distance between the first vertex and each successive vertex is how the Bellman Ford method works. It then iteratively relaxes those estimates by finding new paths that are shorter than the previously exaggerated paths. The Bellman-Ford technique is designed to find the shortest paths between a single source node and all other nodes, even when some edges in a network have negativeweights. Themethodstartsbysettingthedistancetothesourcenodetozeroandthedistances to all other nodes to infinity, signifying that theyare initiallyinaccessible. It then carefullyexamines eachedgeinthegraphtoseewhetherusinganintermediarynodemayshortenthecurrentpathtoa target node. If a shorter path is found, the distance to the destination node is updated. This process, knownasrelaxing, is carried out V-1 times, where V is the number of vertices in the graph, to ensure that all possible paths are considered.

After the relaxation phases, the algorithm does a second pass across the edges to check for any additional distance modifications. If any distance can still be shortened, there is a negative weight cycle,suggestingthatcertainnodeslackafiniteshortestpath.TheBellman-Fordtechniqueishelpful forgraphswithnegativeweightssinceitcannotonlydetermineshortestpathsbutalsodetectnegative weight cycles.

Bydoingthisrepeatedlyforallvertices, we canguarantee that the result is optimize

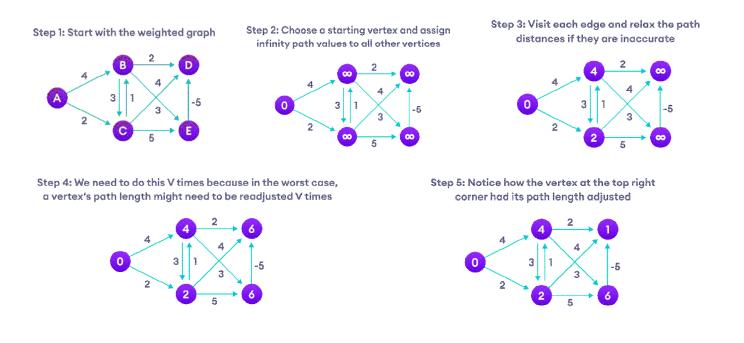


Figure2.exampleofHow BellmanFord'salgorithmwork

C-TheFloyd–Warshallalgorithm

The Floyd-Warshall algorithm is one method for figuringout the shortest paths between each pair of nodes in a network. It uses a dynamic programmingtechnique to determine the shortest paths for the entiregraph, progressively comingup with solutions to smaller subproblems. The method is applicable to both directed and undirected graphs, and is particularly effective for dense graphs. However, the graphmust not have negative weight cycles because this would result in undefined shortest paths. The process begins by initializing a distance matrix, where each entry represents the shortest distance between two nodes. Any directed geconnecting two nodes has its weight put into the matrix. If there

isn'tadirectedge,thedistanceissettoinfinity,makingthenodesinitiallyinaccessibletooneanother. The distance to every node is set to zero since the shortest path between any two nodes is free. The core of the algorithm is its iterative process. Along the paths that connect each other pair of nodes, eachnodeinthenetworkissystematicallyconsideredasapotentialintermediarynode. For everypair ofnodes, it assesses if using this intermediary node provides a shorter paththan the one that is currently knowntoexist.Inthatcase,thealgorithmadjuststhedistancematrixtotakethenew,shorterpathinto consideration. This process is carried out for every node serving as an intermediary point to ensure that all possible paths are considered. At the end of the process, the distance matrix contains the shortestpathsbetweeneachpairofnodes.Additionally,ifanydiagonalmemberinthematrixbecomes negative,thegraph'sweightcycleisshownasnegative.Thisisbecauseanegativecyclewouldrender shortest path calculations invalid for some node pairs, allowing for an indefinitely decreasing path cost. Despite its straightforward methodology, the Floyd-Warshall algorithm is computationally difficult for large graphs, with a time complexity of O(N), where n is the number of nodes. Nonetheless, it is a helpful tool in scenarios like network routing and traffic flow analysis when understandingallpairs'shortestpathsisessentialbecausetoitsuser-friendlinessandabilitytohandle enormous graphs.

D-Johnson'sAlgorithm

Johnson'sAlgorithmisatechniqueforfiguringouttheshortestpathsbetweeneachpairofnodesin a weighted graph. Because it combines the benefits of Bellman-Ford's and Dijkstra's algorithms, it works particularly well with sparse graphs. The unique feature of Johnson's Algorithm is that it can handlegraphswithnegativeedgeweightsaslongastherearenonegativeweightcycles.Thealgorithm first reweights the edges of the graph to eliminate negative weights. The Bellman-Ford algorithm is used to determine the "potential" value of each node, and then all of the graph's edge weights are adjusted. This reweighting ensures that all edge weights become non-negative while preserving the relative order of shortest pathways. The approach uses Dijkstra's algorithm to determine the shortest pathways from each node after reweighting. Since Dijkstra's algorithm works well for networks with non-negative weights, this technique allows Johnson's Algorithm to perform better for sparse graphs than other all-pairs shortest path techniques.

The benefits and drawbacks of traditional shortest path methods are outlined in Table 1. Although it is ineffective with negative edges, Dijkstra's Algorithm works well with dense graphs and non-negative weights. Bellman-Ford is slower and less effective for big, dense graphs, but it can handle negative weights and identify cycles. Floyd-Warshall has a high time and memory complexity for large graphs, yet it can detect cycles and calculate all-pairs shortest paths. Although Johnson's Algorithm works well for sparse networks with negative weights, its reweightingproceduremakes it difficult to use.

Algorithm	Advantages	Disadvantages	
	Efficientforgraphswithnon-negative weights.	Cannothandlenegativeedge weights.	
Dijkstra'sAlgorithm	Guaranteesoptimalsolutionsforsingle- source shortest paths.	Inefficientforverylargeorsparsegraphs	
	Suitablefordensegraphswithnon-negative weights.	without optimizations.	
	Handlesgraphs withnegativeedge weights.	SlowerthanDijkstra's(O(VE))forlarge graphs.	
Bellman-Ford Algorithm	Detectsnegativeweight cycles.		
	Suitablefordistributedsystems	Inefficientfordense graphs.	
	Computesall-pairsshortestpathsinone execution.	Inefficientforlargegraphsdueto $O(V^3)$ time complexity.	
Floyd-Warshall Algorithm	Simpleandeasyto implement.		
	Detectsnegativeweight cycles.	Memory-intensivefordense graphs.	
Johnson'sAlgorithm	Efficientforsparsegraphs.	Complextoimplementdueto reweighting.	
	Handlesnegativeweightswithoutcycles.	Requiresextracomputationfor	
	CombinesthebenefitsofDijkstra'sand Bellman-Ford.	reweighting,addingoverhead.	

Table1. Advantages and Disadvantages of Classical Shortest pathalgorithms types.

2.1.2 Heuristic Shortest PathAlgorithms

Heuristicshortestpathalgorithmsareoptimizationmethodsthatprioritizespeedandefficiencyabove thorough exploration by using heuristic functions to direct the search for paths in a graph. Heuristic approaches aim to approximate optimal paths bymaking well-informed decisions based on expected costs, in contrast to classical algorithms that ensure exact answers.

A-A*Algorithm

A popular heuristic-based approach for determining the shortest path between a source node and a target node in a graph is the A* algorithm. It works especially well in applications with wide search spaces, such game development, robotics, and navigation systems. The A* algorithm balances computational efficiency and optimality by combining the advantages of Greedy Best-First Search and Dijkstra's Algorithm. [13]

A*achieves its performancebyusingacost function to guideits search. The cost function is defined as:

$$f(n) = g(n) + h(n)$$

- g(n) is the actual cost from the start node to the current node n.
- h(n) is the heuristic estimate of the cost from n to the target node.

The heuristic h(n) is a crucial component that establishes the algorithm's efficiency. It must be acceptable (never overstate the genuine cost) in order to guarantee optimal solutions. The method iterativelyinvestigatesnodeswiththelowestf(n)valuetoensurethattheroutesmostlikelytoleadto the target are examined first. If the heuristic is well-designed, A* can significantlyreduce the search spacewhencomparedtoothershortestpathalgorithms.Becauseitenablestheheuristictobetailored forspecificapplications,A*'sversatilityishighlyvaluedbymany.Forexample,in2Dgridnavigation, the Manhattan or Euclidean distance is commonly used as a heuristic. However, the efficacy of the heuristic may decrease in cases where the graph is abnormally large or when the heuristic is poorly chosen [13].

B-GreedyBest-FirstSearchalgorithm

Greedy Best-First Search is a heuristic-based pathfinding method that looks into nodes that seem to be closest to the objective based on a heuristic assessment. "Greedy" refers to its method of continuously choosing the node with the lowest heuristic value in an attempt to reach the goal as quicklyasfeasible.Unlikeotheralgorithms,suchasA*orDijkstra's,whichconsiderboththeexpected cost to theobjective and the cost of accessing anode, GreedyBest-First Search aloneemploys the heuristic function to guide its decisions. The algorithm evaluates its neighbors based on their heuristic values, starting at the source node. After selecting the neighbor that appears to be closest to the goal, it moves to that node. During process, the algorithm iteratively grows then dewith the smallest estimated distance to the destination. Because of its simple, goal-oriented approach, the algorithmcanoftenfind apathtotheobjective quickly, especially insimpleor well-structure dgraphs. However, because greedy best-first search disregards the actual cost of reaching anode, it does not

yield the shortest path. In other cases, the heuristic function may even select a longer, less optimal pathifitproducesestimatesthatarenotcorrect.Forexample,inagraphwithobstaclesordetours,the algorithm can focus on a node that appears closer to the goal but takes a much longer path to get it. This method is particularly useful when speed is more important than precision. In video games, for instance,itiscommonlyemployedtoquicklyguidecharacterstowardadestination.Similarly,inearly searchesorscenarioswithsimpleheuristics,itcanprovideafastestimateofthedesiredpath.Despite itsshortcomings,GreedyBest-FirstSearchiscommendedforitssimplicityandspeedypathdiscovery in large search fields [13].

C-AntColonyOptimization(ACO) algorithm

Ant Colony Optimization (ACO) is a technique that was inspired by the way ants forage for food in the wild. In the wild, ants initially roam around aimlessly, but when they return to the colony after locating food, they leave behind pheromone trails. Other ants, who are more likely to follow paths withhigherpheromoneconcentrations, pickupthese tracks. Eventually, more antsprefer the shortest road since it gathers the most pheromone from frequent use. ACO computationally simulates this behavior to address complex optimization problems, especially those involving paths, such the traveling salesman problem or network routing [14].

Thealgorithminitiallyvisualizestheproblemasagraph,wherenodesrepresentdecisionpoints(e.g., cities on a route) and edges reflect relationships with associated costs (e.g., distances). The graph is traversedbyartificial"ants"that constructs olutions. Each antmakes probabilistic decisions on which

pathtofollownextbasedontwofactors:problem-specificheuristicinformation, suchasthedistance to the next node, and the quantity of pheromone on each edge, which reflects the cumulative desirability of that path. As the ants complete their journeys, the algorithm evaluates the quality of their solutions. The pheromone on less appealing paths is allowed to progressively fade away, while more pheromone is introduced to the edges of paths that lead to better solutions. This evaporation prevents the algorithm from becomingstuck in less-than-ideal solutions byreducingthe influence of suboptimal paths. Over the course of numerous repetitions, the pheromone dynamics guide the ants toward more ideal solutions because shorter or better roads inherently accumulate more pheromone and draw in more ants. One of ACO's primary advantages is its ability to balance exploration and exploitation. At first, the ants' probabilistic decision-making process allows them to explore a range ofoptions, but the pheromonereinforcement gradually focuses on the most promising solutions. As a result, ACO performs particularly effectively in problems with complex constraints or large search spaces.Inthetravelingsalesmanproblem,forexample,wherethegoalistofindtheshortestroutethat visits every city exactly once, ACO can iteratively improve solutions by utilizing the collective behavior of the ants. In a similar vein, network routing can find efficient data transmission paths and adapt dynamically to network changes.

All things considered, Ant Colony Optimization is an intriguing illustration of how strong computational methods can be inspired by natural systems. It is a powerful and adaptable tool for resolving optimization issues in a variety of fields since it can replicate the decentralized and self-organizing behavior of actual ants [14].

Table2outlinestheadvantagesanddisadvantagesofheuristicshortestpathalgorithms.A*guarantees optimal solutions with admissible heuristics but is memory-intensive and heavily reliant on heuristic quality. Greedy Best-First Search is fast and goal-oriented but may produce suboptimal paths and struggle with misleading heuristics. Ant Colony Optimization (ACO) excels in complex, dynamic problems but is computationally intensive and requires careful parameter tuning.

Algorithm	Advantages	Disadvantages	
	Combinesactualcostandheuristicfor optimal solutions.	Performanceheavilydependsonthe quality of the heuristic.	
A *	Guaranteesshortestpathiftheheuristic is admissible and consistent.	Memory-intensiveforlargegraphs.	
	Reducessearchspacecomparedto Dijkstra's.		
CroadyPast First Saarah	Fastandgoal-oriented,oftenreaching the target quickly.	Doesnotguaranteeshortestpath.	
GreedyBest-First Search	Simple to implement.	Cangetstuckinlocalminimaifthe heuristic is misleading.	
	Effectiveforcomplexoptimization problems.	Computationallyexpensiveforlarge problems.	
AntColonyOptimization (ACO)	Flexibleandadaptabletodynamic environments.	Performance depends on parameter	
		tuning(e.g.,pheromoneevaporation	

Table2. Advantages and Disadvantages of Heuristic Shortest PathAlgorithms types.

2.1.3 HybridShortestPathAlgorithms

Hybridshortestpathalgorithmsareanadvancedclassofoptimizationtechniquesthatcombineaspects of heuristic and adaptive strategies like machine learning, genetic algorithms, or dynamic changes with traditional deterministic approaches like Dijkstra's or Bellman-Ford. These algorithms combine the best aspects of heuristic and classical methodologies to achieve the optimal balance between computing efficiency, adaptability, and scalability. They are hence highly effective at addressing difficult pathfinding problems in dynamic and uncertain scenarios.

rate).

Avoids premature convergence by

balancingexplorationandexploitation.

A-MachineLearning(ML)-BasedPathfinding

One of the best-known examples is the hybrid method called Machine Learning (ML)-Based Pathfinding. This approach dynamically selects the optimal routes by utilizing prediction algorithms that have been trained on massive amounts of data. Machine learning algorithms analyze both historical data, such recurring traffic patterns, and real-time inputs, like the amount of congestion at anygiventime,toproducewell-informedroutingdecisions.Forinstance,ML-basedalgorithmsinan intelligent transportation system predict the quickest routes based on real-time traffic, weather, and road closure data. Similarly, by adapting to shifting network conditions, including node failures or bandwidthfluctuations,machinelearning(ML) modelsinInternetofThings(IoT)networksenhance data flow. By incorporating reinforcement learning (RL), a branch of machine learning that enables thesystemtolearnfrompastdecisionsandmakemoreaccuratepredictionsgoingforward,thesystem caniterativelyenhanceitspathfindingtactics.However,thesuccessofML-basedpathfindingdepends on the quality of the training data and the processing capacity available for real-time inference. [15]

B-DynamicA*

AnothercrucialhybridtechniqueisdynamicA*(D*), avariantoftheclassicA*algorithmthatadjusts to modifications in network architecture or edge weights while it is being run. While traditional A* operates on static graphs, D* is designed to adapt in real time. In autonomous robotics, for example, when environmental factors can change abruptly, D* merely recalculates the portions of the path affectedbynewobstaclesorupdatedterraincosts.Insteadofrepeatingtheentireprocess,D*gradually modifiesthesolutiontomaintaincomputingefficiency[17].D*isparticularlywell-suitedfordynamic environments that require continuous adjustment, such urban navigation or disaster response scenarios, because of this feature.

C-GeneticAlgorithm(GA)-BasedPathfinding

GeneticAlgorithm(GA)-BasedPathfindingisanotherinstanceofhybridoptimizationthattakescues from evolution and natural selection. In GA-based pathfinding, which uses a population of potential solutions (paths) that evolves over time, more successful solutions are selected for reproduction and lesssuccessfulonesarerejected.Geneticoperationsthatintroducevarietyandenabletheexploration ofavastsolutionspaceincludemutationandcrossover.Forlargeandcomplexnetworks, such supply chain optimization, logisticsplanning, and network routing, wherethesheernumberofvariablesand constraints may render typical methods impractical, this approach performs very well. GA-based methods require careful parameter tuning, including population size and mutation rate, to ensure convergence to a perfect or nearly ideal solution [16]. The advantages and disadvantages of hybrid shortest route methods are shown in Table 3. Although ML-Based Pathfindingis computationallydemandingand dependent on high-qualitytrainingdata, it can adjust to real-time conditions and learn from past data. Dynamic A* is less appropriate for static graphssinceitintroducescomplexityforincrementalupdateswhileupdatingpathwayseffectivelyin changing settings. Although GA-Based Pathfinding avoids local optima and explores wide solution spaces, it has a slow convergence rate and necessitates exact parameter tweaking.

AlgorithmType	Advantages	Disadvantages	
	-Adaptsdynamicallytoreal-time conditions, such as traffic or network changes.	Computationallyintensive, requiring substantial resources for training and inference.	
ML-Based Pathfinding	Learnsfromhistoricaldatato improveaccuracyovertime.	Performancedependsheavilyonthe	
	Handlescomplex,multi-variable environments effectively.	qualityandvolumeof training data.	
	Efficiently handles changes in graph structure or edge weights withoutrecalculatingfromscratch.	Requires additional logic for incrementalupdates, increasing implementation complexity.	
DynamicA*	Maintainshighcomputational efficiency in dynamic environments.	Notidealforstaticgraphsdueto added	
	Suitableforreal-timenavigation and robotics.	overhead.	
	Capableofexploringlarge, complex solution spaces.	Slow convergence in large-scale problemsduetotheiterativenature.	
GA-Based Pathfinding	Avoidslocaloptimathrough crossover and mutation.	Requires careful parameter tuning	
	Flexibleandadaptabletoawide range of optimization problems.	(e.g.,mutationrate,populationsize)to ensure efficiency.	

$\label{eq:table3.theadvantages} Table 3. the advantages and disadvantages of different types of hybrid shortes tpath algorithms:$

2.2 PerformanceEvaluationofShortestPath Algorithms

Theperformance of shortest pathalgorithms is evaluated using benchmarks such as convergence time, computational complexity, scalability, and fault tolerance, which makes it a crucial area of study. Convergence time quantifies how quickly an algorithm stabilizes routing decisions after network Dijkstra's algorithmisrenowned foritsdeterministic convergence, butheuristic approaches changes. suchasA*concentrateontenableroutestogeneratequickeranswersinspecificsituations[9].Another important statistic is computational complexity. The complexity of Dijkstra's algorithm is $O(V)^{2}$. however with sophisticated data structures like Fibonacci heaps, it can be lowered to $O(V+E) \log(V)$ [13]. By eliminating pointless explorations, heuristic techniques such as A* further optimize this process. Heuristic and hybrid algorithms outperform classical approaches in addressing the problem of scalability, especially in large-scale networks [9]. Fault tolerance is essential in dynamic or disrupted environments. While algorithms like Bellman-Ford are robust to changes in topology, heuristic techniques excel at adapting to changing conditions. Simulation tools such as ns-3 and **OPNET**haveenabledtheevaluationofthesemetricsunderrealisticconditionsandhavealsoprovided insight into the behavior of the algorithms in different scenarios [15].

2.3 EmergingTrends inShortest Path Algorithms

A dvances intechnology have led to changes in algorithms for the shortest path. Machine learning and

artificial intelligence are increasingly being used to dynamically optimize routing decisions. For example, by adaptively learning the optimal routes based on both history and current data, reinforcement learning models improve flexibility in dynamic networks [11]. Thanks to Software-Defined Networking's (SDN) centralized routing control, global shortest path optimization is now feasible. SDN simplifies complex configurations and provides real-time traffic control capabilities, making it a groundbreaking technique in modern networking [15]. Blockchain technology is also changingthegameinthedomainofsecurerouting.Bydecentralizingpowerandensuringtheaccuracy of routing data, blockchain-based protocols minimize securityvulnerabilities, particularlyin IoT and edge networks [6]. Additionally, IoT-specific energy-efficient algorithms address the unique constraints of these devices by emphasizing minimal resource use [8].

2.4 Applications of Shortest Path Algorithms in Modern Networks

Shortest path algorithms, which offer efficient resource management, communication optimization, and routing for a variety of applications, are at the heart of modern networks. These algorithms have evolved to meet the needs of several situations, ranging from traditional wired networks to complex IoT ecosystems and dynamic wireless systems. In traditional wired networks, protocols like RIP (Routing Information Protocol) and OSPF (Open Shortest Path First) heavily rely on shortest path algorithms to maintain optimal routing tables. For example, OSPF uses Dijkstra's algorithm to determine the shortest path tree for each node, ensuringefficient and loop-free data delivery. Similar tothis,RIPfindstheshortestpathsusingtheBellman-Fordalgorithmandhopcounts.Theseclassical methodsareidealfornetworksthatarestaticorsemi-staticandhaverelativelyfewtopologychanges. Node mobility, bandwidth limitations, and dynamic topologies make wireless network challenges morecomplex.Inthiscase,heuristicandhybridalgorithmsworkeffectivelyandadaptquicklyto

changes. Mobile Ad-Hoc Networks (MANETs), for instance, use protocols such as AODV (Ad Hoc On-Demand Distance Vector) to dynamically discover routes only when required. Energy-efficient techniques, such as Ant Colony Optimization or Genetic techniques, are used by Wireless Sensor Networks (WSNs) to enable reliable data transport and prolong the life of devices with limited resources [18]. In the context of the Internet of Things and smart cities, shortest path algorithms are especiallymadetodealwithconstraintslikeenergysavingandadaptation. Algorithmsthatcanpredict and dynamically adapt to network conditions are required since IoT networks usually have limited resources. Due to their ability to learn from historical data and generate real-time routing decisions, machine learning-based pathfinding algorithms are growing in popularity in these scenarios [19]. Applications such as traffic control in smart cities and public transportation depend on shortest path algorithms. For instance, real-time navigation systems include algorithms like A* that dynamically adjust to traffic conditions in order to provide the optimal travel routes. To optimize internal communication, cloud computing and data center environments commonly employ shortest path methods. These systems require efficient routing in order to balance traffic flows and lower latency. Modern data center topologies, such as Clos networks or fat-tree designs, use algorithms like ECMP (Equal-Cost Multi-Path) to effectively distribute traffic across multiple channels [20].

Autonomous systems, including self-driving automobiles, robotic swarms, and drones, use shortest pathalgorithmstonavigateandcompletetasks.AlgorithmslikeDynamicA*(D*)arehighlyhelpful inthis case because they can adapt to changes in the environment in real time, such as the presence of obstacles or dynamic variations in goals. This adaptability ensures safe and efficient travel in unpredictablesituations.Byselectingroutesthatmaximizethroughputandminimizelatency,shortest path algorithms optimize data flow in telecommunication networks. For example, MPLS (Multiprotocol Label Switching) networks use shortest path techniques to establish efficient data channels across big, interconnected systems. Critical infrastructure, such as electricity grids and emergency response systems, can also benefit from these algorithms. Power networks use shortest pathalgorithmstominimizetransmissionlosses and ensurereliable distribution of electricity. During emergencies, these algorithms help determine the optimal escape routes and prioritize the restoration of communication networks. Moreover, shortest path methods are crucial to applications in artificial intelligenceandmachinelearning. They are used in recommendation systems to analyze relationships inuser-itemgraphsandinsocialnetworkanalysistomeasureindividualinfluenceandconnectedness [20]. In these diverse applications, the value and versatility of shortest path approaches are demonstrated. They enable systems to adapt, enhance, and function reliably even in complex and dynamic environments. By combining classical, heuristic, and hybrid approaches, these algorithms continue to encourage innovation and ensure the seamless operation of modern networks.

3Literature Review

S.JohnsonandM.Keller,[13]suggestedsimulationtoolstoassesstheeffectivenessofshortestpath algorithms,likeMininetandOMNeT++.Thesetoolsofferaccuratesettingsfortestingfaulttolerance, scalability, and efficiency in a range of network scenarios. Their research emphasizes how crucial simulation is for connecting theoretical models with practical applications.

R.Floyd,[14]presentedtechniquesfordynamicprogrammingtoaddressall-pairsshortestpathissues. Thisseminalworkestablishedthefoundationforcontemporaryalgorithmsusedintrafficanalysisand worldwide connection by demonstrating effective processing in dense graphs. Floyd's approach continues to have an impact on the development of comprehensive pathfinding applications.

M. L. Garcia and P. Martinez, [15] examined developments in shortest path algorithm simulation methodswithanemphasisonscalabilityinmassivedynamicnetworks.Theirworkdemonstratedhow simulationscanbeusedtoanalyzealgorithmperformanceundervaryingnetworkloads,whichmakes it possible to create reliable routing solutions.

M. A. Javaid, [16] gave a thorough explanation of Dijkstra's method, highlighting its effectiveness and simplicity in static topologies. The algorithm's shortcomings in dynamic contexts wereshown by the analysis, which led to more investigation into a daptive techniques. Javaid's observations are still applicable in situations involving organized networks.

X. Z. Wang, [17] compared the effectiveness of the Dijkstra, Bellman-Ford, and A* algorithms in both static and dynamic networks. Wangprovided helpful advice forchoosingthe best method for particularnetworksettingsbyidentifyingtrade-offsbetweencomputingcomplexity, accuracy, and flexibility.

J. Kleinberg and É. Tardos, [18] discussed sophisticated algorithmic techniques for shortest path problemsthatarebasedongraphs. Theirresearchdemonstrated computationally effective and scalable methods that are suited to the growing needs of contemporary networks. The study forms the basis for creating novel routing strategies.

T.H. Cormen et al., [19] discussed thetheoretical foundations and real-worldapplications of classic algorithms like Bellman-Ford and Dijkstra's. Their research serves as a vital resource for comprehending the mathematical underpinnings of shortest path algorithms and how they are implemented.

A.Orda, [20] models that address congestion and delay in time-dependent networks for shortest path computation. The study offered ideas for enhancing routing in both static and dynamic systems by introducing adaptive techniques for real-time traffic and dynamic network situations.

K. R. Chowdhury and I. F. Akyildiz, [21] created a routing protocol that optimizes spectrum consumption for cognitive radio ad hoc networks by utilizing shortest path methods. Their research showed how flexible shortest path techniques may be in controlling limited network resources and improving overall effectiveness.

X. Yang and D. Mehdi, [22] examined improvements to network virtualization shortest path techniques. In order to guarantee scalability and effective resource allocation, they addressed the difficulties in handling changing topologies and virtualized resources and offered solutions.

M. Al-Karaki and A. Kamal, [23] Reviewed routing techniques in wireless sensor networks, emphasizing energy-efficient shortest path algorithms. Their research helped to ensure the sustainability of WSNs by addressing the need for dependable communication with resource conservation in limited devices.

X. Sun et al., [24] presented secure routing systems for Internet of Things networks based on blockchain technology. The study made sure that shortest path calculations were transparent, trustworthy, and impervious to manipulation by incorporating blockchain technology. The potential of decentralized security solutions in network routing is demonstrated by their methodology.

R. Xu, H. Zhou, and Y. Zhang, [25] presented a framework for adaptive shortest path routing in complicated networks using reinforcement learning. Their methodology reduces latency and increases routing efficiency by dynamically adapting to changes in real time. This AI-powered method establishes a standard for contemporary routing methods.

A. Goyaletal.,[26]createdagraph-basedmodelfordynamicshortestpathcomputingthatcombines deep learning and reinforcement learning. The study showed flexibility in large-scale networks and decreased processing cost. Their research highlights how AI might improve routing efficiency.

B. Lee et al., [27] created a hybrid shortest path algorithm that combines swarm intelligence and heuristic techniques for VANETs. Their program outperformed conventional techniques in terms of efficiency and adaptability by optimizing routing in crowded situations by utilizing real-time traffic data.

C. Zhangetal., [28] suggested a multi-objective optimization paradigm for Internet of Things systems that balances dependability, latency, and energy usage. Through the use of a genetic algorithm with Pareto optimality, their work made it possible to route data effectively in situations with limited resources.

D. Wang et al., [29] addressed k-shortest path issues in extensive road networks by using graph attentionnetworks(GATs). Theirmodelshowedpromiseforurbantrafficmanagementsystemswhere effective routing is essential and increased prediction accuracy.

E. Chen et al., [30] created amachinelearning-based adaptiveshortest path techniqueforSDNs that can dynamically anticipate and reduce congestion. Their method improved network utilization and throughput, which helped SDNs scale.

F. Liu et al., [31] suggested a shortest path technique that runs faster on a GPU for real-time smart cityapplications. Their approach greatlydecreased processingtime byemployingCUDA to parallelize computations, allowing for effective pathfinding in large-scale graphs.

G. Roy et al., [32] presented a hybrid routing algorithm for MANETs that combines Bellman-Ford and Dijkstra's advantages. Their method improved stability and computational efficiency by dynamically switching between algorithms according to network conditions.

H. Xu et al., [33] discussed shortest path calculations in wireless sensor networks that take energy efficiency into account. The model extended network lifetime by optimizing routes while taking energy consumption and replenishment rates into account by incorporating a reinforcement learning framework.

I. Singh et al., [34] suggested a real-time shortest path algorithm that uses reinforcement learning to adjust to traffic circumstances in real time for intelligent transportation systems. The algorithm demonstrateditsefficacyincontemporarytrafficnetworksbydrasticallyloweringaveragetriptimes.

J. Pateletal.,[35]createdashortestpathalgorithmforhigh-dimensionalnetworksthatisinspiredby quantum mechanics. Their approach showed excellent scalability and computational efficiency by mimickingquantumannealingprocesses,providingcreativeanswerstochallengingroutingproblems.

Table 4 provides an overview of the evaluated literature. A thorough summary of numerous studies on shortest path algorithms and their uses in various network contexts is given in this table. It emphasizes significant innovations, approaches, and methods used to tackle issues like scalability, resource restrictions, and dynamic environments. Table 8, which arranges this corpus of work, is a useful resource for comprehending developments in shortest path calculations, such as traditional algorithms, heuristic techniques, and reinforcement learning frameworks.

Reference	Focus/Topic	KeyContributions	Algorithm(s) Used
[21]	Simulation tools (OMNeT++,Mininet)	Evaluated performance of shortest path algorithmsundervaryingnetworkconditions, highlightingtheroleofsimulationinbridging theory and practice.	Dijkstra's,Bellman- Ford
[22]	Dynamicprogramming for all-pairs shortest paths	Introducedefficientcomputationmethodsfor dense graphs, laying foundational work for modern pathfinding algorithms.	Floyd-Warshall
[23]	Advancesinsimulation techniquesfordynamic networks	Highlighted the role of simulations in analyzingalgorithmscalabilityandrobustness under dynamic network loads.	Heuristic and simulation-based approaches

Table4. Summarization of Literature review

[24]	AnalysisofDijkstra's algorithm	Emphasized its simplicity and efficiency in staticnetworkswhileidentifyinglimitationsin dynamic environments.	Dijkstra's
[25]	Comparative study of Dijkstra,Bellman-Ford, and A* algorithms	Evaluated trade-offs in computational complexity, accuracy, and adaptability for static and dynamic networks.	Dijkstra's,Bellman- Ford, A*
[26]	Advancedgraph-based algorithmic strategies	Discussedscalable,efficientsolutionstailored for modern network demands, serving as a cornerstoneforinnovativeroutingapproaches.	Graph-basedalgorithms (general strategies)
[27]	Reviewofclassical algorithms	Detailedtheoreticalandpracticalapplications of Dijkstra's and Bellman-Ford algorithms.	Dijkstra's,Bellman- Ford
[28]	Time-dependentshortest paths	Proposed models addressing latency and congestioninreal-timedynamic networks.	Time-dependent variationsofshortest path algorithms
[29]	Routing in cognitive radioadhocnetworks	Optimizedspectrumusageusingshortestpath algorithms, enhancing adaptability and efficiency in resource-constrained environments.	Dijkstra's,heuristic- based algorithms
[30]	Enhancements for networkvirtualization	Proposed solutions for managing dynamic topologiesandvirtualizedresources, ensuring scalability.	Hybrid algorithms
[31]	Energy-efficientrouting in wireless sensor networks	Addressed resource conservation in constrained devices while ensuring reliable communication.	Energy-awareshortest path algorithms
[32]	Blockchain-based routingprotocolsforIoT	Ensuredtransparency,trust,andresistanceto tampering in shortest path computations, enhancing security in network routing.	Blockchain-enhanced shortestpath algorithms
	•		

[33]	Reinforcementlearning for adaptive routing	Developed an AI-driven framework for dynamically adjusting routes in complex networks, improving efficiency and reducing latency.	Reinforcementlearning- based shortest path algorithms
[34]	Graph-based models integrating deep and reinforcementlearning	Demonstrated adaptability in dynamic networkswhilereducingcomputational overhead.	Deep learning and reinforcementlearning
[35]	Hybridalgorithmfor VANETs	Combinedheuristicandswarmintelligence methods for efficient routing in congested scenarios.	Swarmintelligenceand heuristic algorithms
[36]	Multi-objective optimizationforIoT systems	Balanced energy consumption, latency, and reliability using genetical gorithms and Pareto optimality.	Geneticalgorithms
[37]	Graph Attention Networks(GATs)fork- shortest paths	Improvedpredictionaccuracyforurbantraffic management in large-scale road networks.	Graph attention networks(GATs)
[38]	Adaptivealgorithmsfor SDNs	Incorporatedmachinelearningtodynamically predict and mitigate congestion, enhancing scalability.	Machinelearning-based shortestpath algorithms
[39]	GPU-accelerated shortestpathalgorithm	Reducedprocessingtimesignificantlyforreal- time applications in smart cities through CUDAparallelization.	Parallelized shortest pathalgorithms(GPU- based)
[40]	Hybridroutingfor MANETs	DynamicallyswitchedbetweenDijkstra'sand Bellman-Ford algorithms based on network conditions,improvingstabilityandefficiency.	Dijkstra's,Bellman- Ford
[41]	Energy-awareroutingin WSNs	Optimizedroutesconsideringenergy consumption and replenishment, extending networklifetimeusingreinforcementlearning.	Energy-awareand reinforcementlearning algorithms
[42]	Real-timeshortestpath algorithm for ITS	Leveraged reinforcement learning to dynamicallyadapttotrafficconditions, significantly reducing travel times.	Reinforcementlearning- based algorithms
[43]	Quantum-inspired shortestpathalgorithms	Demonstrated superior scalability and efficiency for complex, high-dimensional networksusingquantumannealingprocesses.	Quantum-inspired shortestpathalgorithms

4. Discussion

The ability of shortest path algorithms to strike a balance between computing efficiency and adaptability while dealing with intricate network routing problems is among their most alluring features. The deterministic nature and dependability of classical algorithms, such Dijkstra's and Bellman-Ford, in static networks are highlighted by research conducted by [21] and [24]. Bellman-Ford expands the applicability of Dijkstra's method to include situations with negative edge weights, while Dijkstra's approach is especially praised for its effectiveness in graphs with non-negative weights. Their shortcomings, however, become apparent in dynamic networks where real-time flexibilityisimpededbytherequirementforrecalculations. Webelievethatwhileclassical algorithms are very useful for clearly specified, static issues, they are not flexible enough for contemporary, dynamicsystems.Bybringingflexibilityandheuristic-drivenefficiency,heuristicalgorithmssuchas AandAntColonyOptimization(ACO)*,on theotherhand.providecreativesolutions.Accordingto [13],A*isperfectforapplicationslikeroboticsandnavigationbecauseitcombinesheuristicforecasts with actual costs to guarantee optimal solutions. However, ACO, which was evaluated by [14], uses biological inspiration to optimize pathways in large-scale, adaptive networks in a dynamic manner. Although these algorithms perform exceptionally wellindy namic contexts, their generalizability may beconstrained by their dependence on heuristic quality (for A*) and computing complexity (for ACO). Fordynamicandlarge-scalesystems, webelieve heuristical gorithms offer a substantial advance over conventional approaches; yet, they still need to be carefully tuned to reach their full potential.

Shortestpathoptimizationhasgone further with the introduction of hybrid algorithms, which combine theadvantagesofheuristicandclassicalmethods.Forinstance,DynamicA*,whichwasexaminedby [17], greatly increases the efficiency of real-timenavigation systems by including incremental updates to adaptively recalculate just affected courses. Similarly, reinforcement learning is used in machine learning(ML)-basedpathfinding, as discussed in [19] and [25], to dynamically forecast the bestroutes. MLbased techniques provide unmatched scalability and flexibility, and they perform very well in highdimensional and data-rich environments. However, they are difficult to apply in systems with limitedresources duetotheirneedon largeamountsoftraining dataand computationalpower.Since hybrid algorithms combine the flexibility of heuristic and machine learning-driven techniques with the accuracy of traditional methods, we believe they are the way of the future for shortest path optimization. The possibility of sustainability in shortest path algorithms is another fascinating analogy. Energy-efficient routing, fueled by algorithms like ACO and ML-based models, can lower powerconsumptioninIoTnetworks, according to studies like [32] and [38]. These developments are in line with network management's increasing demand for sustainable technologies. Heuristic and hybrid incorporate energy conservation, which makes them more applicable techniques in contemporary applications than classical algorithms, which only concentrate on pathoptimization. We believe that this emphasis on sustainability not only makes these algorithms more useful, but also guarantees that they are in line with more general environmental objectives.

Although these algorithms have advanced, there are still difficulties in putting them into practice. Concerns including interpretability, scalability, and the moral ramifications of automated decision-making are highlighted in research by [35] and [37]. For instance, despite their strength, ML-based algorithmshavea"black-box"aspectthatmakesitchallengingtocomprehendorjustifytheirchoices. On the other hand, while traditional algorithms such as Dijkstra's are more visible, they are not as flexible as machine learning-based solutions. For researchers and practitioners, striking a balance between transparency and adaptability continues to be a crucial task.

4.1 Comparing the differences between Shortest pathalgorithms types

Table5comparesClassical,Heuristic,andHybridshortestpathalgorithms,focusingontheirstrengths and applications. Classical algorithms like Dijkstra's and Bellman-Ford guarantee accuracy but strugglewithdynamicgraphsandlarge-scaleproblemsduetotheircomputationalintensity.Heuristic algorithmslikeA*andACOprioritizeefficiencybyguidingthesearchwithapproximationsbutmay produce suboptimal paths if the heuristic is flawed. Hybrid algorithms combine the precision of classical methods with the adaptability of heuristics or machine learning, excelling in dynamic and complex environments, though they are computationally demanding. Each category fits specific use cases, from static graph analysis to real-time navigation in IoT systems. The choice depends on the trade-offs between accuracy, efficiency, and adaptability.

Aspect	ClassicalAlgorithms	HeuristicAlgorithms	HybridAlgorithms
Approach	Deterministic and mathematically grounded methodsthatguaranteeoptimal solutions.	Use approximations and heuristicstoguidethesearch, improving efficiency.	Combine deterministic methodswithheuristicor adaptive techniques for better performance.
Types	Dijkstra's,Bellman-Ford, Floyd-Warshall	A*,GreedyBest-FirstSearch, Ant Colony Optimization (ACO)	Machine Learning-Based Pathfinding,DynamicA*, Genetic Algorithm (GA)- Based Pathfinding
Optimality	Guaranteestheshortestpath under specified conditions.	Oftenprovidesnear-optimal pathsbutdoesnotguarantee the shortest path.	Balancesbetweenoptimality and efficiency, often achieving near-optimal solutions.

 Table5. Comparing the differences between Classical, Heuristic, and Hybridshortes tpath algorithms:

Efficiency	Can be computationally expensiveforlargegraphsor dynamic environments.	Moreefficientduetoheuristic- driven search, reducing unnecessary exploration.	Achieves high efficiency by combiningclassicalprecision with heuristic adaptability.
Adaptability	Lessadaptabletodynamic changes; requires recomputation if graph changes.	Can adapt to dynamic conditionsbutdependsheavily on the heuristic used.	Highlyadaptabletodynamic environments, often capable of real-time updates.
Complexity	Moderatecomplexity, often $O(V)$ or $O(V^2)$ depending on the algorithm.	Complexity depends on the heuristic;typicallylowerfor static graphs.	Higher complexity due to combining methods but offersbetterscalabilityand adaptability.
SearchStrategy	Exhaustiveexplorationofall possible paths to guarantee correctness.	Focusesonthemostpromising paths based on heuristic estimates.	Integratesheuristicguidance with deterministic calculations or adaptive learning.
MemoryUsage	Requires significant memory forstoring allpaths and costs.	Requireslessmemorydueto reduced search space.	Memory-intensive due to combined techniques and storageofadditionallearning parameters.
Applications	Networkrouting,staticgraph analysis, distributed computations.	Navigationsystems,robotics, dynamicrouting,and games.	Complex optimization problems, real-time navigation,IoTnetworks, and multi-agent systems.
KeyStrengths	Accuracyandreliability;well- suited for static and well- defined problems.	Speed and efficiency, especiallyinlargesearch spaces or dynamic environments.	Flexibility,scalability,and adaptability to changing conditions.
Key Weaknesses	Pooradaptabilitytodynamic graphs and computationally intensive for large-scale problems.	Heuristic quality impacts solutionquality;suboptimal paths are possible.	Higher computational and implementationcomplexity dueto combiningmethods.

4.2 Comparing the differences between Classical algorithms types

Table 6 compares four shortest-path algorithms based on their purpose, edge weight handling, complexity, and use cases. While Dijkstra's Algorithm performs best on sparse graphs with non-negative weights, Bellman-Ford handles graphs with negative weights and detects negative cycles. Floyd-Warshallefficientlydeterminesall-pairsshortestpathsfordensegraphs,despiteitsprocessing demands.Forsparsenetworksthatrequireall-pairsshortestpaths,Johnson'sAlgorithmcombinesthe Bellman-Ford and Dijkstra algorithms. Each algorithm has pros and cons, and the requirements and graph topology determine which algorithms are applicable.

4.3 ComparingbetweenHeuristicShortestPathAlgorithmstypes.

Based on their methodology, effectiveness, and use cases, A*, Greedy Best-First Search, and Ant Colony Optimization (ACO) are contrasted in Table 7. Although A* is memory-intensive, it guarantees optimal pathways with accepted heuristics by striking a balance between actual costs and heuristics. For speed, Greedy Best-First Search just uses heuristics, but it runs the risk of choosing less-than-ideal routes. ACO is computationally demanding yet excels at complicated, dynamic situationsthankstoitsuseofpheromonesandprobabilisticexploration.Greedyisbestforquick,easy searches, A* is best for optimal navigation, and ACO is best for large-scale optimization such as

searches, A* is best for optimal navigation, and ACO is best for large-scale optimization such as network routing and TSP. ACO stands out for its parallelism, which uses several agents to conduct exploration.

Aspect	Dijkstra'sAlgorithm	Bellman-Ford Algorithm	Floyd-Warshall Algorithm	Johnson's Algorithm
Purpose	Finds the shortest path fromasinglesourcetoall nodes.	Finds the shortest pathfromasingle source to all nodes.	Findstheshortest pathsbetweenall pairs of nodes.	Findstheshortest pathsbetweenall pairs of nodes.
EdgeWeights	Non-negativeweights only.	Handles both positive and negativeweights.	Handles both positive and negativeweights (nonegative cycles).	Handlesbothpositive andnegativeweights (no negative cycles).
Cycle Detection	Doesnotdetectnegative weight cycles.	Detectsnegative weight cycles.	Detectsnegative weight cycles.	Detects negative weightcyclesduring reweighting.
TimeComplexity	$O(V^2+E)$ OR $O((V+E)\log V)$ Withpriorityqueue.	O(VE)	O(V ³)	$O(VE+V^2LogV)$

Table6. Comparing the differences between Dijkstra's Algorithm, Bellman-Ford Algorithm, Floyd-
Warshall Algorithm, and Johnson's Algorithm:

GraphType	Bestforsparsegraphs with non-negative weights.	Works for any weighted graph (withoutnegative cycles).	Suitablefordense graphs.	Bestforsparse graphs.
Space Complexity	O(V+E) foradjacencylist implementation.	O(V+E) foradjacencylist implementation.	<i>O</i> (<i>V</i> ²) duetothedistance matrix.	$O(V^2)$ due to reweighting anddistancematrix.
Approach	Greedyalgorithm.	Dynamic programmingwith edge relaxation.	Dynamic programmingwith incremental updates.	Combines Bellman- Fordforreweighting and Dijkstra's for pathfinding.
UseCase	Bestforroutinginstatic networks with non- negative weights.	Used for distributed systemsorgraphs withnegative weights.	Used for dense graphs or when all-pairs shortest pathsare required.	Efficient for sparse graphsandall-pairs shortest paths.
Implementation Complexity	Simple to implement.	Relativelysimple to implement.	Simple but computationally intensive.	Complex due to reweighting and multiplealgorithms.

Table7. Comparing between A*, Greedy Best-First Search, Floyd-Warshall Algorithm, and Ant Colony Optimization (ACO):

Aspect	A *	GreedyBest-First Search	AntColonyOptimization (ACO)
Approach	Combines actual cost $g(n)$ and heuristic estimate $h(n)$ to find the short est path.	Reliessolelyon the heuristicestimateh(n)to guide the search.	Usespheromonetrailsand heuristic information for probabilistic pathfinding.
Optimality	Guaranteestheshortestpath iftheheuristicisadmissible and consistent.	Does not guarantee the shortest path, as it only focusesontheimmediate goal.	Doesnotalwaysguaranteethe shortest path but often finds near-optimal solutions.
SearchStrategy	Expandsnodesbasedon f(n) = g(n) + h(n) balancingexplorationand exploitation.	Expands nodes based on thesmallestheuristic value $h(n)$ favoring goal-directed paths.	Explores multiple paths probabilisticallyandreinforces better solutions with pheromones.

Complexity	Memory-intensiveforlarge graphs due to maintaining open and closed lists.	Requires less memory comparedtoA*butmay explore irrelevant paths.	Computationallyintensivefor large-scale problems due to multipleiterationsand pheromone updates.
Performance	Highlyefficientwithawell- designedheuristic,reducing unnecessary exploration.	Fasterinsimplegraphsbut prone to getting stuck in suboptimal paths if the heuristicis misleading.	Balances exploration and exploitation, making it effectiveforcomplex,dynamic problems.
Heuristic Dependency	Strongly depends on the heuristic for efficiency but guaranteescorrectnesswith admissible heuristics.	Fully relies on the heuristic, making its accuracycriticaltothe algorithm's success.	Partially dependent on heuristic;pheromonedynamics compensate for heuristic weaknesses.
Parallelism	Sequential, typically processesonepathatatime.	Sequential,focusingon one path at a time.	Highly parallelizable, as multipleantscanexplorepaths simultaneously.
Applications	Usedinnavigation,robotics, and scenarios requiring optimal paths.	Common in quick pathfinding,likevideo games,wherespeedis more critical than accuracy.	Idealforcomplexoptimization problems, such as TSP, network routing, and dynamic systems.

4.4 ComparingbetweenHybirdShortestPathAlgorithmstypes.

Table 8 contrasts the use cases, complexity, and flexibility of ML-Based Pathfinding, Dynamic A*, andGA-BasedPathfinding.ML-BasedPathfindingusesmachinelearningtoforecastthebestroutes; it works well in dynamic settings but needs a lot of trainingdata and processingpower. Dynamic A* adds overhead for static issues but ensures optimalityin real-time scenarios such as robot navigation by incrementally adapting graph changes. Despite its delayed convergence and need on parameter tuning, GA-Based Pathfinding effectively explores vast, complicated networks by applying evolutionary principles. Dynamic A* is effective in adaptive scenarios, GA flourishes in large-scale, intricate optimization tasks, and ML shines in high-dimensional domains.

		D	
Aspect	ML-BasedPathfinding	DynamicA*	GA-BasedPathfinding
Approach	Uses machine learning models (e.g., neural networks, reinforcement learning)topredictoptimal pathsbasedonhistorical and real-time data.	ExtendstheA*algorithmto handle changes in graph topology or edge weights during execution, adapting incrementally.	Uses principles of natural selection (mutation, crossover,andselection)to evolve paths toward an optimal solution.
Adaptability	Highlyadaptivetodynamic environments by learning from data and adjusting in real-time.	Adaptsdynamicallytochanges in the graph without recalculating the entire path.	Adaptive through population evolutionbutlessresponsive to real-time changes comparedtoMLorDynamic A*.
Optimality	Provides near-optimal solutions,dependingonthe qualityof trainingdata and model accuracy.	Guarantees optimality in dynamic environments if changesarehandledcorrectly.	Does not guarantee the shortest path but can find near-optimalsolutionsfor complex problems.
Complexity	Computationallyintensive dueto model trainingand inference requirements.	Moderatecomplexity;efficient indynamicgraphsbutrequires additional logic for incremental updates.	Computationallyexpensive for large problems due to iterative evolution and evaluation of populations.
KeyLimitation	Requires high-quality training data and computationalresourcesfor training and inference.	Lesseffectiveforstaticgraphs due to additional overhead for incremental updates.	Convergence can be slow, andperformancedependson carefully tuned parameters.
SearchSpace	Learnstooptimizeinhigh- dimensional and multi- variable spaces.	Focusesonlyonportionsofthe graph affected by changes, reducing unnecessary recalculations.	Exploreslargesearchspaces by evolving solutions, makingitsuitableforhighly complex networks.
Parallelism	Parallelizable for prediction tasks,especiallywhenusing distributed machine learning.	Sequentialbutefficientin focusing onlyon relevant graph changes.	Highly parallelizable, as multiple solutions (populations)canbeevolved simultaneously.

${\it Table 8. Comparing the differences between {\tt ML-Based Path finding, Dynamic A*, and GA-Based Path finding:}$

Applications	Intelligenttransportation systems.	Dynamicenvironmentslike robotnavigationorurban exploration.	Logisticsandsupplychain optimization.
	Real-timeIoTnetwork optimization.	Disasterresponseandadaptive routing.	Networkroutingforlarge, complex systems.
	-Autonomousnavigation (e.g., drones, vehicles).		Schedulingandresource allocation.
Heuristic Dependency	Reliesonpredictivemodels rather than explicit heuristics.	Requiresaheuristictoestimate path costs, similar to standard A*.	No explicit heuristic; solutionsevolvebasedon fitness evaluation.

Whencomparingshortestpathalgorithms,traditionaltechniquessuchasBellman-FordandDijkstra's areeffectiveanddependableinstaticsituationsbutineffectiveindynamic,adaptivenetworks.Greater flexibilityand scalabilityareprovided byheuristic algorithms like A* andACO, which perform well in dynamic systems but need careful tweaking. Lastly, by fusing accuracy with flexibility and sustainability, hybrid algorithms such as Dynamic A* and ML-based models offer the most reliable results. We believe that hybrid algorithms, particularlythose based on machine learning, provide the most promising way forward. They are perfect for complex, dynamic systems because they provide scalability and flexibilitythat are unrivaled byheuristic and classical approaches. But in the end, the particular application will determine which algorithm is best, taking sustainability, adaptability, and computational efficiency into account.

Conclusion

In network optimization, shortest path techniques are essential for striking a balance between scalability, flexibility, and efficiency. Traditional algorithms, such Bellman-Ford and Dijkstra's, function well in static networks but poorly in dynamic ones. Although they mostly rely on heuristic quality, heuristic approaches such as A* and Ant Colony Optimization effectively and adaptably handletheseproblems.Precisionand flexibilityarecombinedinhybridtechniques, such as Dynamic A*andmachinelearning-based algorithms, which perform well in complicated and dynamic situations but demand a large amount of processing power. Hybrid approaches that combine the advantages of machine learning, heuristic, and classical methods are the way of the future for shortest path algorithms. Promising avenues for enhancing security, scalability, and computational efficiency are provided by emerging technologies like block chain and quantum computing. These developments will guarantee that shortest path algorithms remain relevant in meeting the needs of contemporary networksby redefining their function. These algorithms will continue to play a crucial role in facilitating effective, flexible, and dependable network communication across a range of applications by overcoming present constraints and integrating sustainability.

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